# Gas flow around luminous protoplanets in the context of planet migration

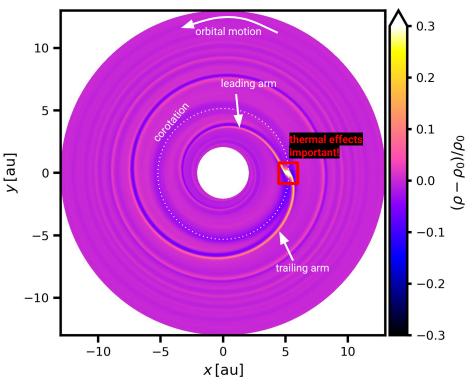
# results from Chrenko & Lambrechts (2019)

Ondřej Chrenko Charles University, Prague chrenko@sirrah.troja.mff.cuni.cz https://sirrah.troja.mff.cuni.cz/~chrenko CPDs II Conference, 15 Mar 2021

#### Outline

Based on results from Chrenko & Lambrechts (2019) I will

- **review thermal effects** that operate in the vicinity of planets and affect their migration
  - cold-finger effect (Lega et al. 2014)
  - heating torque (Benítez-Llambay et al. 2015)
- describe the 3D distortion of the gas flow around luminous planets
- show that the flow can become non-stationary, causing an oscillatory migration



### **3D model**

• hydrodynamic module of **Fargo3D** (Benítez-Llambay & Masset 2016) + equations for energy densities of radiation and gas (following Bitsch et al. 2013):

radiative diffusion  

$$\frac{\partial E_{\rm R}}{\partial t} + \nabla \cdot \mathbf{F} = \rho \kappa_{\rm P} \left[ 4\sigma T^4 - cE_{\rm R} \right], \qquad \text{absorption/emission coupling}$$

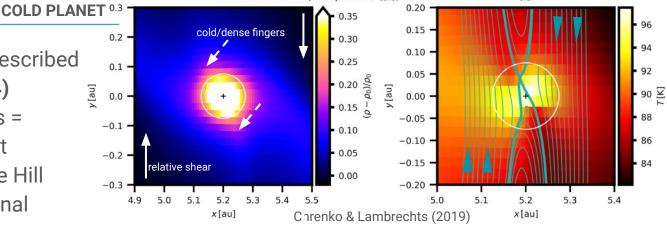
$$\frac{\partial \epsilon}{\partial t} + (\mathbf{v} \cdot \nabla) \epsilon = -P \nabla \cdot \mathbf{v} - \rho \kappa_{\rm P} \left[ 4\sigma T^4 - cE_{\rm R} \right] + Q_{\rm visc} + Q_{\rm art} + Q_{\rm acc}, \qquad \text{viscous and shock heating}$$

$$\frac{\partial \epsilon}{\partial t} + (\mathbf{v} \cdot \nabla) \epsilon = -P \nabla \cdot \mathbf{v} - \rho \kappa_{\rm P} \left[ 4\sigma T^4 - cE_{\rm R} \right] + Q_{\rm visc} + Q_{\rm art} + Q_{\rm acc}, \qquad \text{accretion heating of protoplanets (as in Benitez-Llambay et al. 2015)}$$

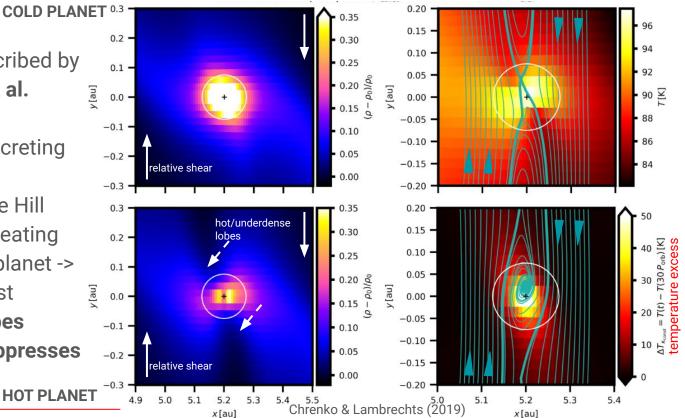
- 3 M<sub>Earth</sub> planet at 5.2 au: **non-accreting** (zero luminosity) or **accreting**  $L = \frac{GM_pM_p}{R_p} = \frac{GM_p}{R_p\tau}$ (mass doubling time 100 kyr, luminosity 4.2x10<sup>27</sup> erg s<sup>-1</sup>)
- opacity: constant or Bell & Lin (1994)

# Constant-opacity disk: review of thermal effects

- cold-finger effect described by Lega et al. (2014)
- cold = non-luminous = non-accreting planet
- gas flow through the Hill sphere: compressional heating -> radiative energy loss -> decompression -> internal energy deficit
- cold/dense fingers
- negative torque (supports inward migration)



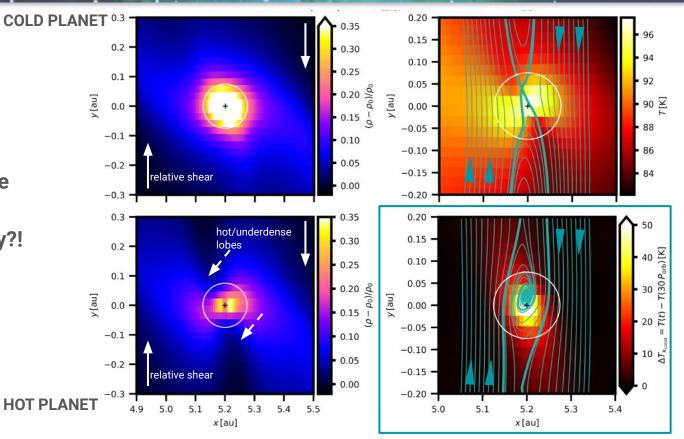
# Constant-opacity disk: review of thermal effects



- heating torque described by Benítez-Llambay et al. (2015)
- hot = luminous = accreting planet
- gas flow through the Hill sphere: additional heating from the luminous planet -> internal energy boost
- hot/underdense lobes
- positive torque (suppresses inward migration)

# Constant-opacity disk: a new result

• But what causes the differences in the streamline topology?!

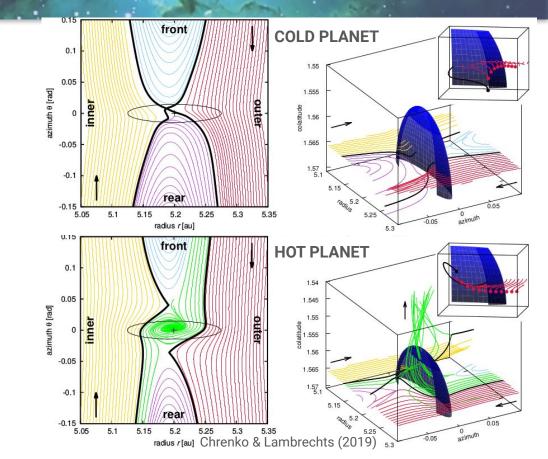


### **Constant-opacity disk: streamline topology**

For the hot planet we see:

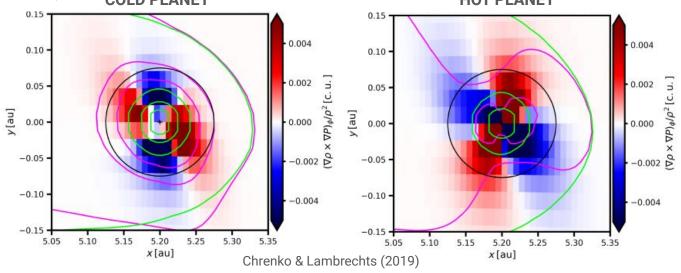
- a **vertical outflow** from the Hill sphere (note that cold & low-luminosity planets have an inflow; e.g. Lambrechts & Lega 2017)
- U-turns farther away from the Hill sphere
- circulating streamlines bend towards the planet and rise vertically

flow perturbations explained in the following...



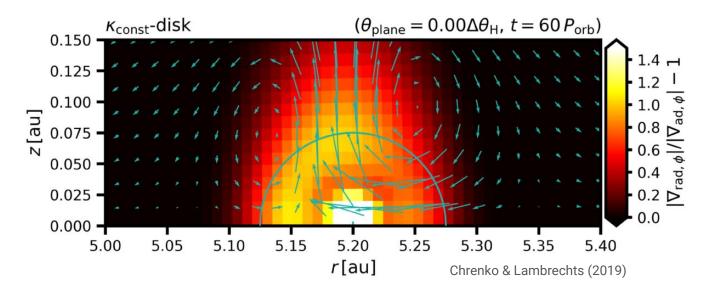
#### **Baroclinic flow perturbation**

- baroclinic term of the vorticity equation:  $\frac{\nabla \rho \times \nabla P}{\rho^2}$
- for the hot planet: surfaces of constant density (purple) and pressure (green) substantially misaligned; map of the baroclinic term antisymmetric (compared to the cold planet)
   HOT PLANET



#### **Convective flow perturbation**

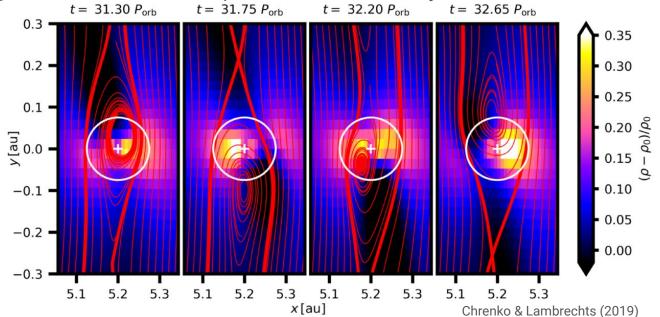
• vertical map of the Schwarzschild convective criterion  $\frac{|\nabla_{\text{rad},\phi}|}{|\nabla_{\text{ad},\phi}|} - 1 > 0$  for the hot planet:



# Disk with a temperature-dependent opacity

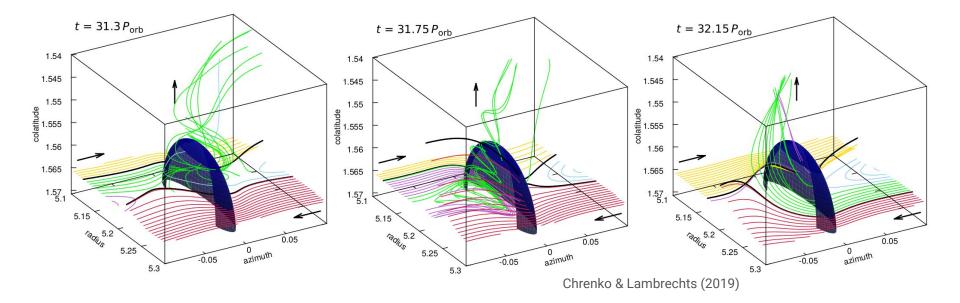
• When the disk opacity is changed from constant to temperature-dependent... (opacity $\sim T^2$  behind the water-ice line according to Bell & Lin 1994)

... the gas flow around the hot planet is not stationary!!!



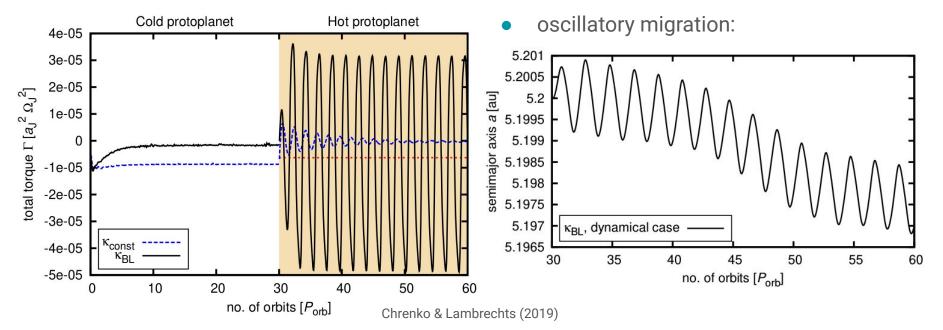
### Non-stationary flow in 3D

• as on the previous slide but in 3D



#### Implications for planet migration

• blue curve ~ the constant-opacity disk; black curve ~ the disk with Bell & Lin's opacity



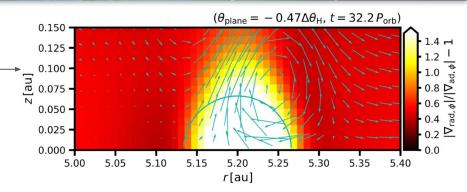
# Why is the flow non-stationary?

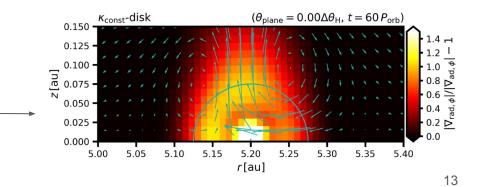
- Schwarzschild criterion for the simulation with temperature-dependent opacities —
- the background is already super-adiabatic

$$\left( \frac{|\nabla_{\mathrm{rad},\phi}|}{|\nabla_{\mathrm{ad},\phi}|} - 1 \right)_{\mathrm{background}} = \frac{1/(4-\beta)}{(\gamma-1)/(\gamma)} - 1$$
  
~0.67 for  $\beta$ =2,  $\gamma$ =1.43 (e.g. Ruden & Pollack 1991)

• Thus the hot planet can excite convective perturbations over an extended region

For a comparison, this is what we saw for the constant-opacity case





#### Conclusions

#### Takeaways:

- Radiative effects can dominate the orbital evolution of low-mass protoplanets
- Gas flow around a luminous (accreting) protoplanet exhibits features (i.e. vertical outflow; streamline distortion) that do not exist for non-luminous planets
- Depending on the background disk model, the flow can become non-stationary and the migration oscillatory

#### (Some) open questions:

- How is the accretion heat deposited/released? How does the flow through the Hill sphere connect to the planetary envelope?
- What luminosity is reasonable to expect? Is pebble accretion dominant for *L*; or perhaps mergers of low-mass planetary embryos?